

Need astronomical, compact mass
to generate detectable GW (exercise 11)

EHLERS 2018 L4P1

↳ Astrophysics of compact bodies

~~what~~ stars → not so compact, hot due to nuclear burning
what happens when a star burns its fuel?

no thermal pressure to counter gravity

↳ collapse, with mass ejection (sometimes: explosion, supernova)

... until degeneracy pressure takes over

(Fermions \downarrow Pauli principle + Compton-wavelength $\propto \hbar/m$)
dominant pressure from lightest particle
(longest wavelength) \downarrow electrons!

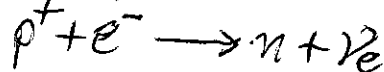
↳ white dwarfs

but: they have a maximum mass $\sim 1.5 M_{\odot}$!
(Chandrasekhar mass)

more mass \downarrow further collapse!

\downarrow very high pressure

\downarrow inverse β -decay becomes energetically favorable



\downarrow degeneracy pressure from neutrons

↳ neutron stars

again: have a max. mass $\gtrsim 2 M_{\odot}$ $\hat{=}$ initial mass

more mass \downarrow further collapse

20-30 M_{\odot}

↳ black holes

most interesting for GW: black holes & neutron stars

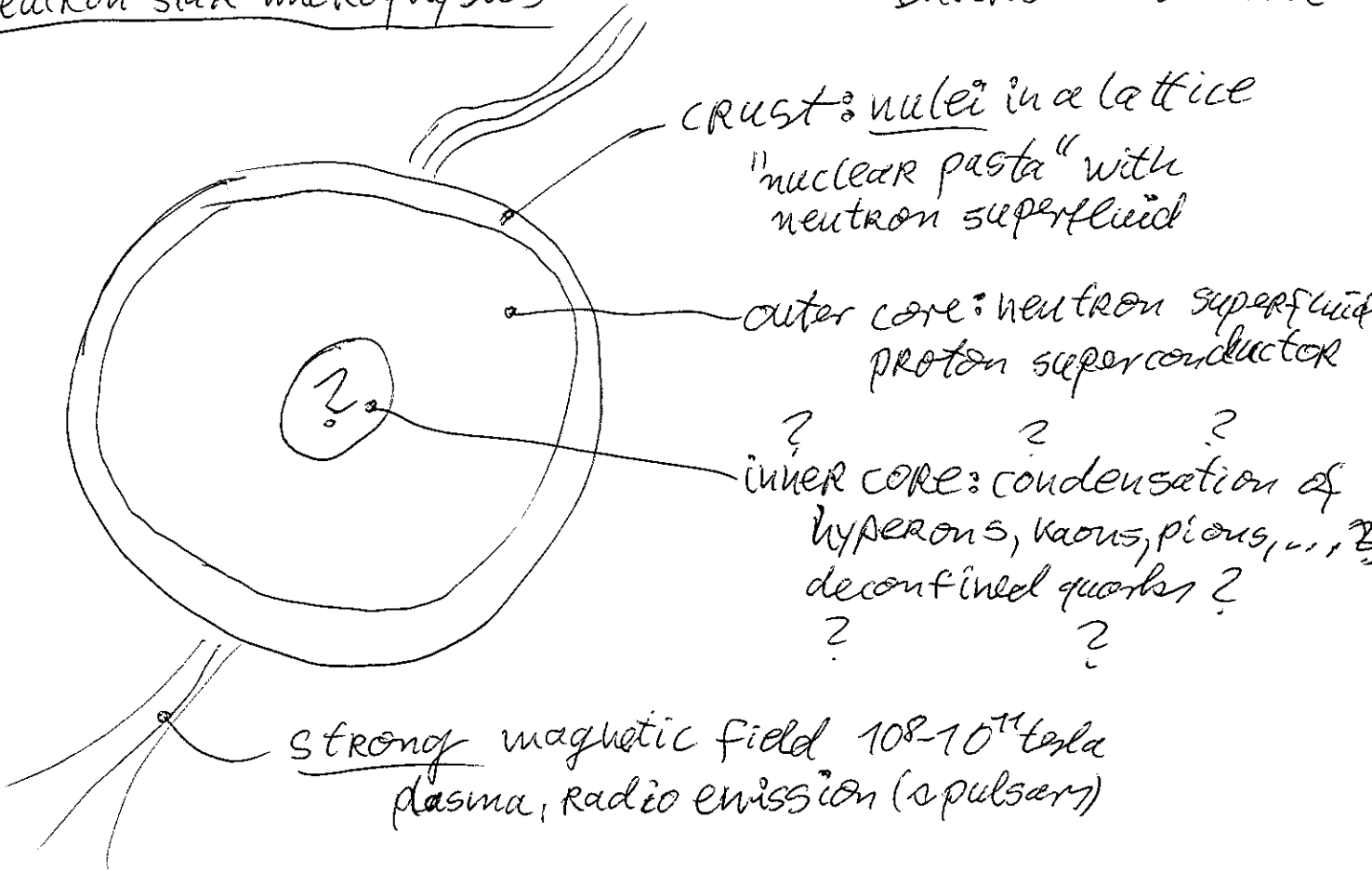
black holes → lectures by Maria Rodriguez

Modeling neutron stars:

Einstein equations + hydrodynamics + equation of state
(+symmetries) (ideal fluid) \hookrightarrow microphysics

neutron star microphysics

Ehlers 2018 L4P2

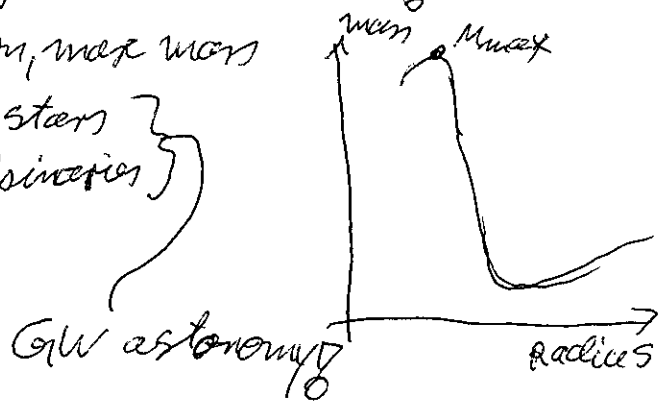


other properties: $10\text{km} \lesssim$ neutron star radius $\lesssim 15\text{km}$
 mass $1-2 M_{\odot}$
 \sim the sun compressed to the size of a city
 \sim a teaspoon of neutron star matter 10^{13} kg \sim a mountain

open problem: e.g. observed $2 M_{\odot}$ neutron star incompatible with predicted condensation of hyperons \sim hyperon problem

How can one solve these problems? \sim observations!

- mass-radius relation, max mass
- "mountains" on neutron stars
- tidal deformation in binaries



Another question for GW astro?

how do compact binaries form?

\hookrightarrow challenges: (from binary stars)

- asymmetric supernova \sim recoil ("kick") \sim binary could disrupt
- star towards death expands \sim common envelope phase \sim might be eaten by companion



Good sources of GW:

- binaries with black holes, neutron stars
- mountains on rotating neutron stars
- supernova (asymmetric)
- big bang
- surprises?

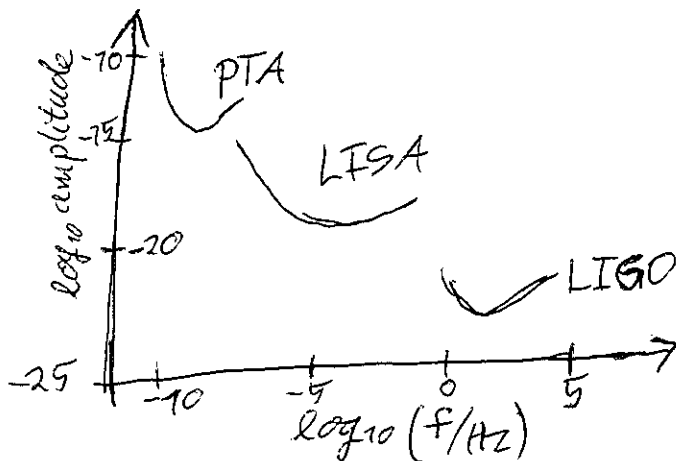
GW astronomy & precision physics

↳ since GW basically ~~don't~~ don't get disturbed on their way to detector!

- important exceptions:
- cosmological redshift
 - gravitational lensing
 - ↳ (de-) magnification, phase perturbations
 - or same signal arrives multiple times!

GW Detectors

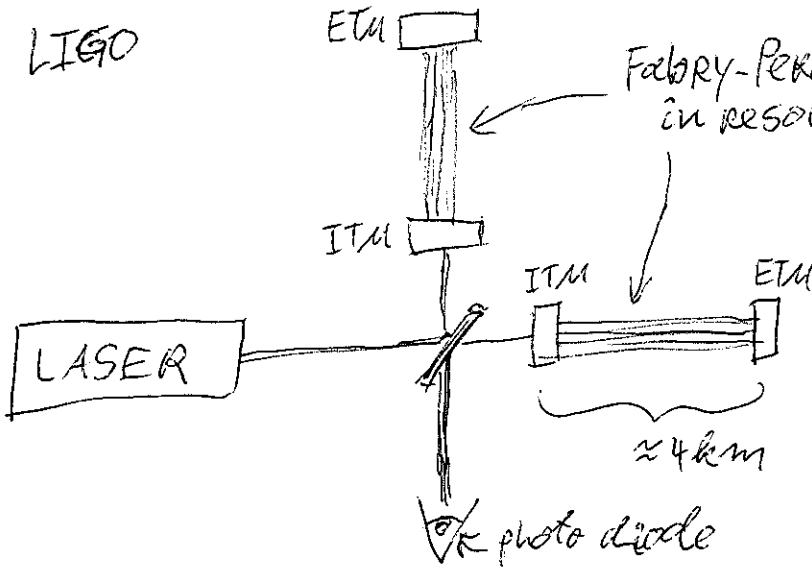
- ground-based detectors (interferometers)
 - LIGO (USA), Virgo (Italy) } "2nd generation"
 - future: Kagra (Japan), LIGO India } ~ 4 km
 - 3rd generation? ~ 10-30 km
- pulsar timing ARRAYS (PTA) 2020's
 - ↳ including the Square kilometre Array (SKA)
- LISA space mission 2034



also: GW signatures

in the cosmic microwave background & Planck, Bicep2 & nothing found

- bar detectors "Weber bars"



Fabry-Pérot cavities
in resonance, Finesse ≈ 450

\approx Michelson-Interferometer

GW make relative arm
length change \rightarrow changed
interference at diode

4 test-masses: 2x ITM, input test mass } 34 x 20 cm
2x ETM, end test mass } fused silica
40 kg

test-masses are "free falling" in horizontal direction

\rightarrow approximately valid for frequencies > 10 Hz due
to ~~geometric~~ suspension \rightarrow seismic isolation,
damps forces by 10 orders of magnitude

complicated instrument: hundreds of feedback control
loops keep interferometer in "lock"
(eg. Fabry-Pérot in resonance)

sensitivity: $h \sim 10^{-21}$ $\rightarrow \Delta L = 10^{-13}$ ~~cm~~ $\sim \frac{1}{1000}$ proton radius ∇

incredible experimental
achievement!